

PHYS 393
Low Temperature Physics
Set 7:

Low Temperature: Cooling Techniques

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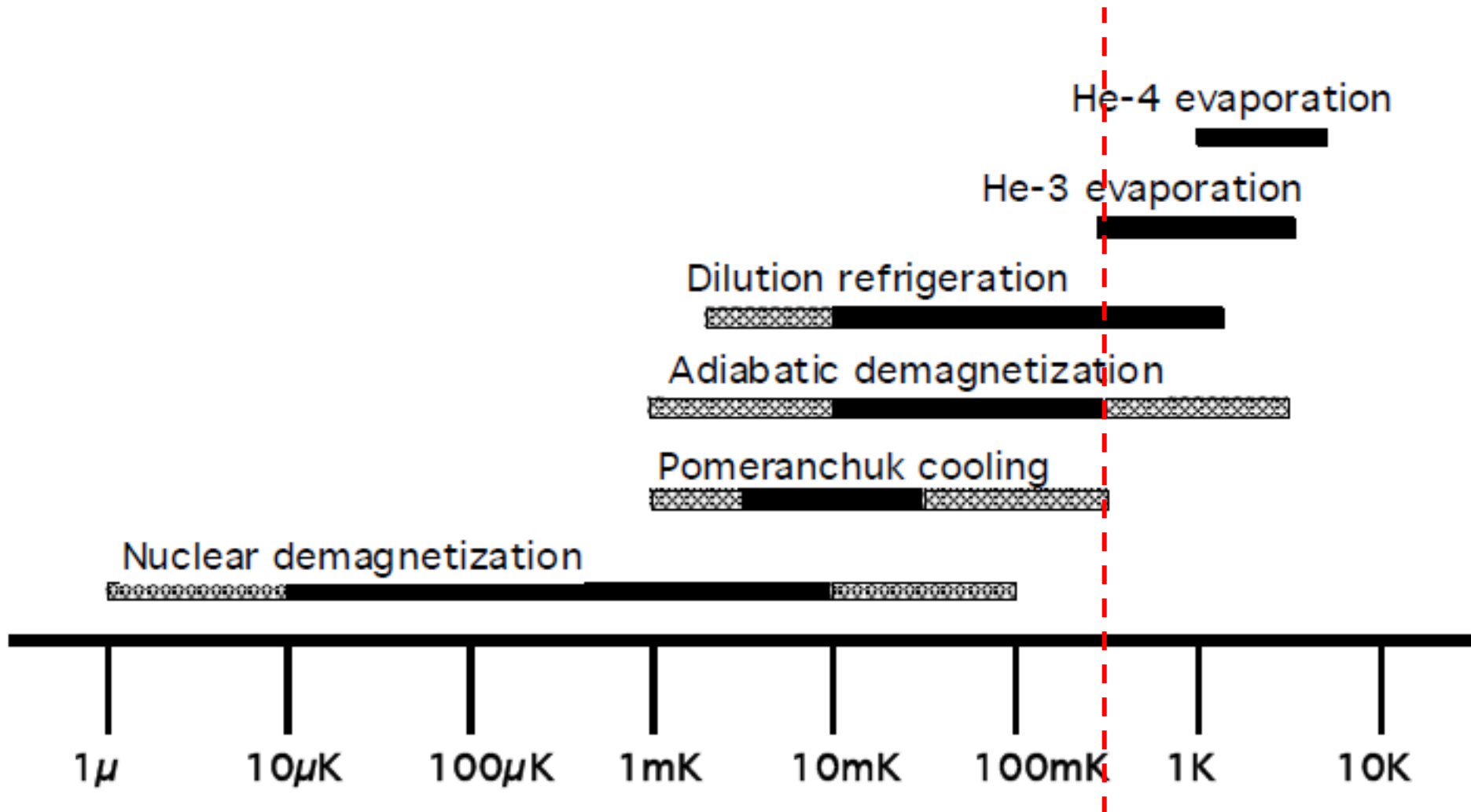
Gas liquefaction and refrigeration

- Standard cooling technique for $300 < T < 4.2\text{K}$: cryogenic liquids (Nitrogen, Helium) obtained from liquefaction
- Oxygen liquefaction: 1877
- Helium liquefaction: 1908
- Varying vapour pressure over He^3 bath allows to maintain down to 0.3K

Substance	T_b/K
CO_2	195
CH_4	112
O_2	90.2
N_2	77.4
H_2	20.3
^4He	4.21
^3He	3.19

Boiling temperatures at atmospheric pressure

Temperature and Cooling Methods



Temperature, Energy, Entropy

- Temperature T usually related to Energy U
- At low temperature it is more helpful to associate Temperature T to Entropy S
- Recall: Entropy $S = k \ln \Omega$
 - Ω = number of microstates of system
 - Quantitatively Ω represents the disorder in the system
- In equilibrium system as $T \rightarrow 0$ system goes to ground state $\Omega=1$ and $S=0$
 - But energy U is not 0 (ground state energy)

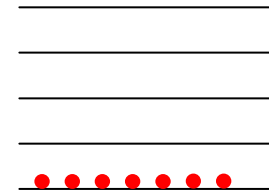
U, S at T=0

- System of N bosons
 - Bosons condense into ground state

$$T \rightarrow 0$$

$$U \rightarrow 0 \quad (\text{ignoring zero point energy})$$

$$S \rightarrow 0$$

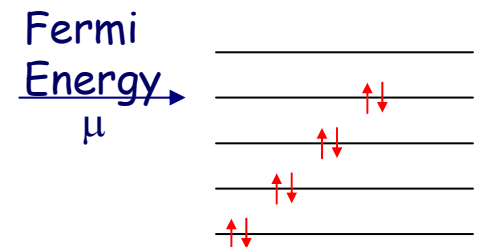


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- System of N electrons (Fermions)
 - Electrons condense to lower set of states (Pauli principle)

$$T \rightarrow 0$$

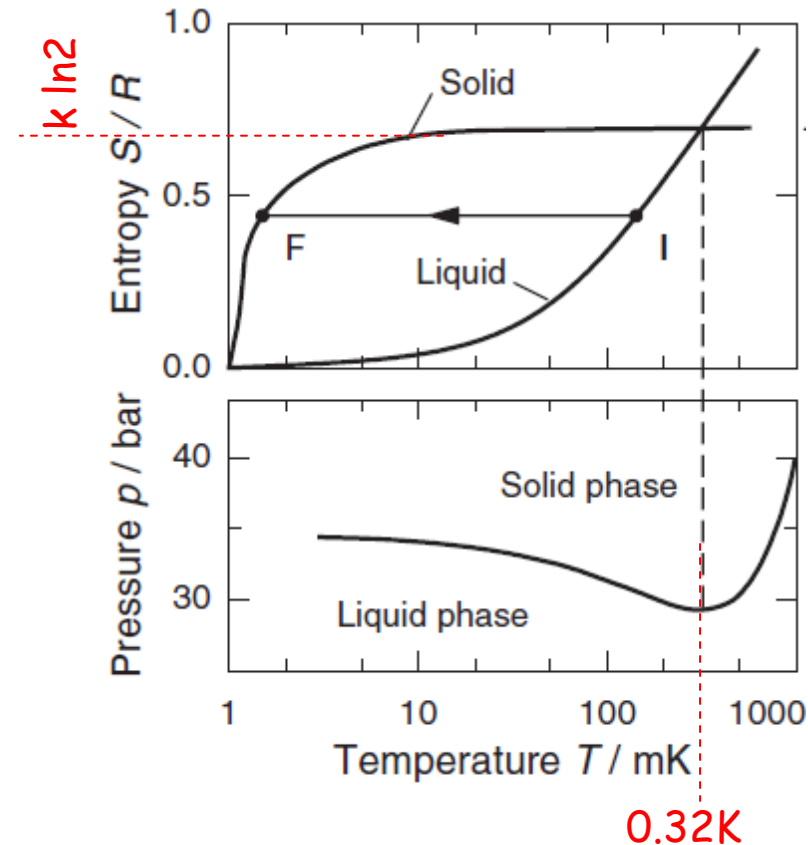
$$U \rightarrow \frac{3}{5} N \mu$$

$$S \rightarrow 0$$



Pomeranchuk cooling (1K to 1mK)

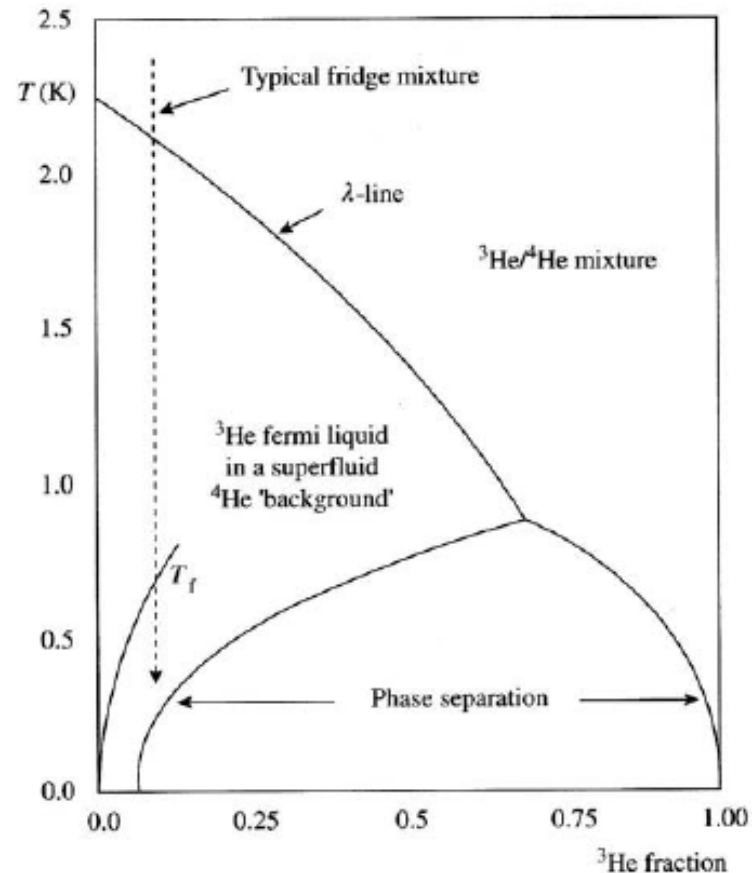
- Working substance: He^3
- $2\text{mK} < T < 0.32\text{K}$: entropy of liquid less than entropy of solid (Low Temperature notes 1, p. 13-16)
- Nuclear spins in solid (localized atoms) more disordered than liquid
- Compress adiabatically (I to F): temperature drop from T_I to T_F
- Takes place in thermally insulated cell
- Sample to be cooled is attached to the cell



Note logarithmic x-axis

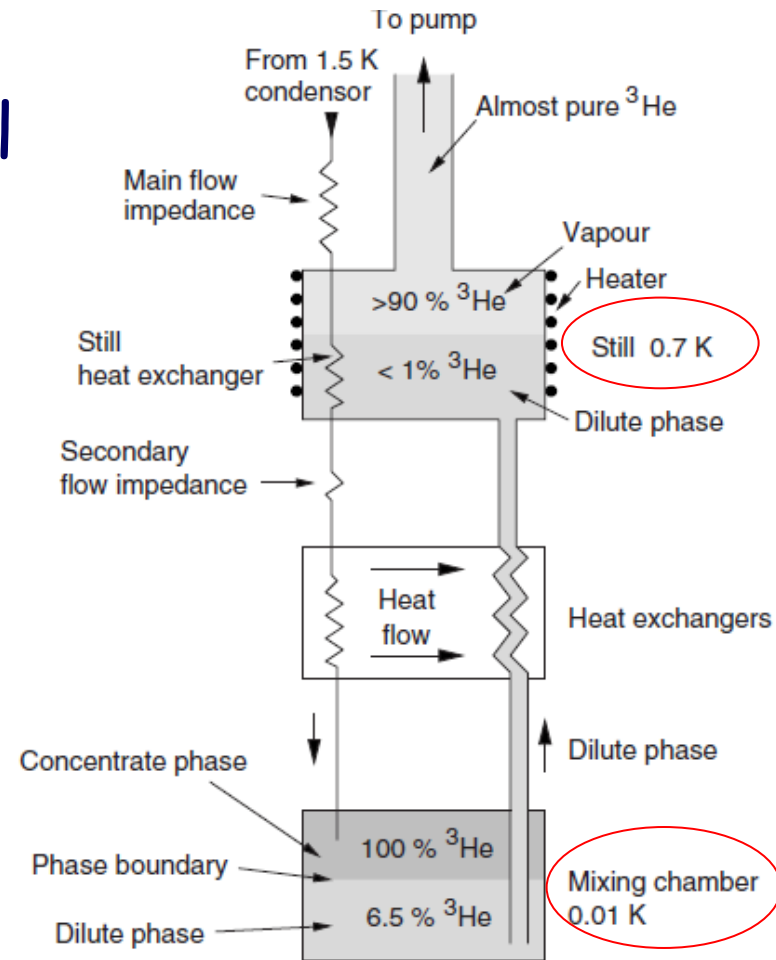
He³/He⁴ Dilution Refrigerator

- Main method to cool to ~1mK
- Phase separation below 0.86K (Low Temperature notes 5, p. 3-5): Layer of pure He³ floats on top of layer of ~6% He³ in He⁴
- He⁴ at this temperatures is 100% superfluid
- He³ in He⁴: free gas in massive vacuum
- He³ has higher entropy in He⁴ dilute phase than in pure He³
- When He³ crosses boundary from pure He³ into dilute phase its entropy increases, hence it absorbs heat
- Similar to evaporation
- The trick is to make this “evaporation” happen



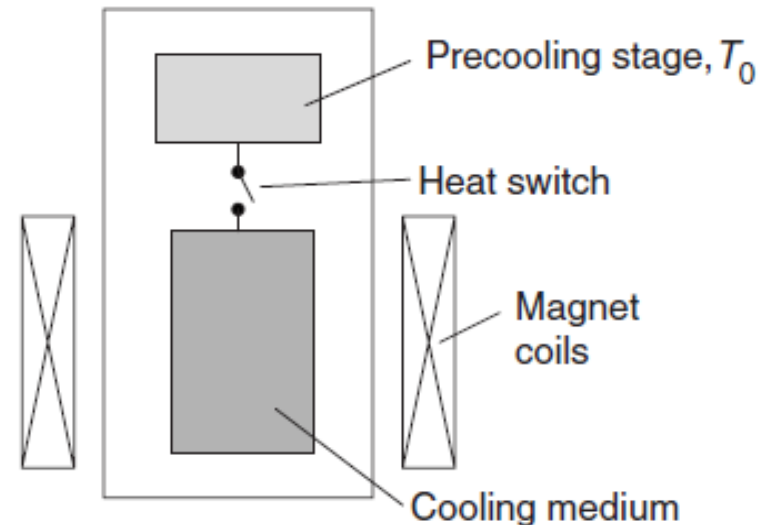
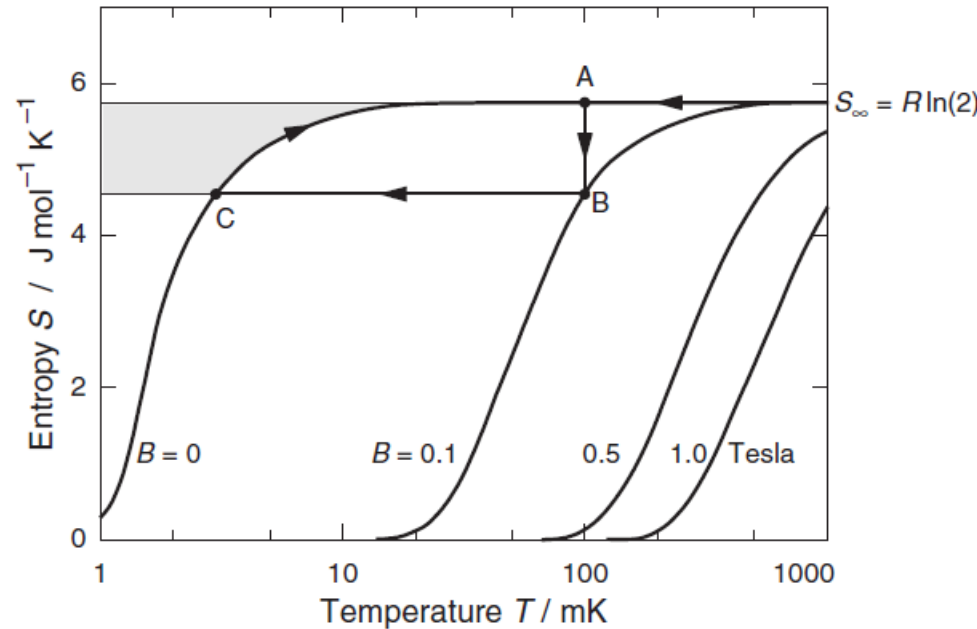
Dilution refrigerator

- Cooling happens in mixing chamber
- Dilute phase connected to still
- Vapour pumped out of still (preferentially He^3 due to higher vapour pressure)
- Purified
- cooled in still (0.7K)
- cooled in heat exchanger (mK)
- returned to the pure He^3 phase



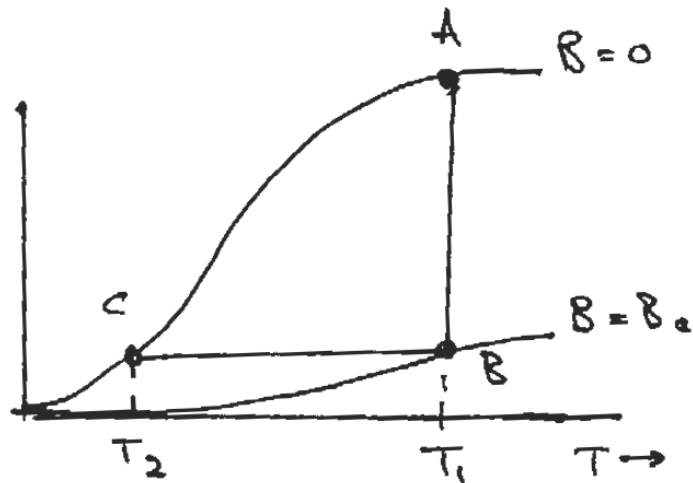
Adiabatic demagnetization

- Relies on magnetic field dependence of spin entropy
- Principle: pre-cool sample; use B field to align spins (reduces entropy releasing heat); isolate thermally, switch B field off: system cools (path ABC)
- Cooling via adiabatic demagnetization of atomic magnetic moments used since 1933
- Reaches temperatures down to 1mK

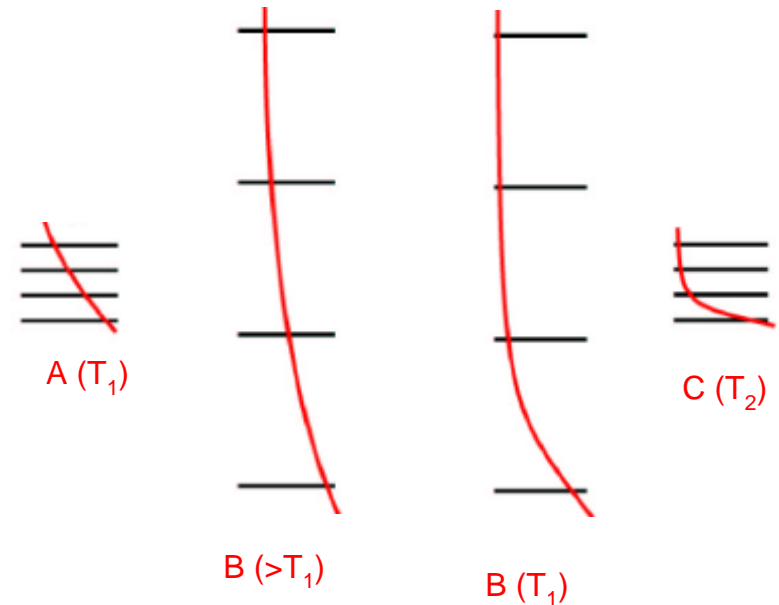


Nuclear Adiabatic Demagnetization

- Nuclear Spin Polarization: mK \rightarrow μ K
- Metallic copper (^{63}Cu , spin 3/2)



1. Magnetize sample isothermally at T_1 (A to B) - Achieved with sample connected thermally to heat sink
2. Isolate thermally the sample
3. Demagnetize adiabatically (B to C)



A : almost degenerate states, similar populations
 B ($>T_1$) : large energy gaps, higher total energy (temperature rise)
 B (T_1): Large energy gaps, larger population in lower states to keep energy content constant (isothermal magnetization)
 C (T_2): lower energy states, population shifted to lower states compared to A, thus lower temperature